Model Checking Multiple Logs

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The Seventh Annual Digital Forensic Research Workshop

Presented by: Mohamed Saleh
1. Log Systems and Digital Forensics
   - Use Case
   - Challenges

2. Combining and Correlation of Logs
   - System Setup

3. Modeling Combined Logs
   - Log Events
   - Log Trees

4. Verification of Properties
   - Logic
   - Verification
Objectives

Problem statement:
Given an IT system with logs collected from various heterogeneous sources, can we reconstruct the events leading to a system failure.

We need to clarify what properties we expect from:

- Logs.
- Heterogenous sources.
- Events.
Clarifications

Logs
A log is a *stored* sequence of *events*. It originates from a certain system, and each event is a string containing information about a certain action of interest that occurred in this system.

Heterogeneous sources of logs
Logs may originate from various systems such as different operating systems or different networking equipment. These systems may have different rules for generating, storing or transmitting logs.

Log events
An event is a string that describes an action that occurred in the log source. It must have a *time-stamp* and contain information about the action and the identity of the entity that carried it out.
An Abstract View

Combined Logs → Analysis

Unifying Formats

Log Source → Synchronization
Log Source → Synchronization
Log Source → Synchronization

Synchronization
A Scenario

Log permanent storage

Network

Log
Log
Log
Log
A Scenario

Log permanent storage

Investigation

Network

Attack

Log

Log

Log

Log permanent storage
Goal and Challenges

From the previous discussion some of the issues are:

- Synchronization of time stamps between different log sources.
- Integrity of logs.
- Security of logs during transmission.
- Unifying formats from different log sources.
- Correlating logs from different sources for forensic purposes.
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- Correlating logs from different sources for forensic purposes.
Combining Logs

- Log events have heterogenous formats
- Normalizing produces events with a common format.
- Normalized events are combined and stored.
- Stored events are time-stamped and their sources are known.
Our objective is to analyze and correlate log events.

Model checking is a good formal solution.

A suitable model for logs is developed.

Properties are expressed in a suitable logic.

But .. What model? and What logic?
Our objective is to analyze and correlate log events.

Model checking is a good formal solution.

- We are searching for patterns of events.
- Patterns are often expressed in formal languages.
- The search then amounts to model checking.

A suitable model for logs is developed.

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Multi-sorted Term Algebras

Digression: Multi-sorted Algebra

⇒ Starting from:
  - A set of sorts \( \{s_1, s_n, \ldots \} \).
  - For each sort \( s' \):
    - A set of variables of the sort.
    - A set of function symbols \( f : s_1 \times s_2 \ldots \times s_n \to s' \) of arity \( n \), where \( n \geq 0 \).
    - Function symbols of arity 0 are called constants of sort \( s' \).

⇒ The set of terms of sort \( s' \) contains:
  - All variables of sort \( s' \).
  - All terms \( f(t_1, \ldots t_n) \) where \( f \) is a function symbol \( f : s_1 \times s_2 \ldots \times s_n \to s' \) and each \( t_i \) is a term of sort \( s_i \).

The multi-sorted term algebra is the set of terms of all sorts.
An example of an algebra

- Sorts: \( \{ \text{int}, \text{bool} \} \)
- Variables of sort \( \text{int} \): \( x_i, y_i, \ldots \) and of \( \text{bool} \): \( x_b, y_b, \ldots \)
- Function symbols of sort \( \text{int} \): \( \{ \text{add}, 0, 1 \} \), where \( \text{add} : \text{int} \times \text{int} \rightarrow \text{int} \) and 0 and 1 are constants.
- Function symbols of sort \( \text{bool} \): \( \text{compare} : \text{int} \times \text{int} \rightarrow \text{bool} \)

All the following are terms of the term algebra:

- \( \text{add}(x_i, y_i), \text{add}(0, 1), \text{add}(z_i, 1) \)
- \( \text{compare}(x_i, y_i), \text{compare}(\text{add}(0, 1), 1), \text{compare}(z_i, 1) \)
Event and Log Models

- Each normalized log event is modeled as a term of a term algebra.
- The function symbols represent action, and the parameters provide information about this action.
- The combined log itself is modeled as a tree.
- Edges of the tree are the algebraic terms representing log events.
- Starting from the root, events appear from oldest to the most recent.
- Concurrent events appear as two branches at the same level.
Model for Log Events

A log event is modeled as a term of a term algebra with variables.

\[ \text{ProcessExit} : \text{process} \times \text{user} \rightarrow \text{bool} \]

Function symbol “ProcessExit”, sorts of domain and codomain are shown.

\[ \text{Logon} : \text{user} \times \text{userID} \times \text{group} \times \text{domain} \times \text{process} \times \text{logonType} \rightarrow \text{bool} \]

Function symbol (Operation) “Logon”.

Example:

- The term \( \text{ProcessExit}(p_1, u_x) \) means user \( u_x \) terminated process \( p_1 \).
Examples of Events

We can think of a large number of events, we can mention:

- **User-related events:**
  - *Logon, Logoff*, etc.
- **Process-related events:**
  - *ProcessBegin, ProcessExit*, etc.
- **Network-related events:**
  - *Get, Post*, etc.

Each of these can be represented by an appropriately designed function symbol from the algebra. The parameters of each function symbol should convey required information about the event. How about logs of events?
A log is modeled as a tree whose edges are terms of a term algebra.

Events

- Logon(…)
- ProcessBegin(…)
- ObjectOperation(…)
- LogOff(…)

Time

- e₀ to e₂ are concurrent.
- All terms contain no variables (are ground terms).
- How to describe properties of the tree?
Expressing Properties of Log Trees

Overview

Given a log tree whose edges are ground terms of the term algebra, we would like to search it for suspicious patterns of events.

The questions now are:

- How to express these patterns?
- How to express occurrences of patterns?
- How to search the tree?
Examples of Patterns

Some of the patterns we may be interested to look for:

- Signatures of known attacks.
- For every “Logon” of some user $u_x$ there should be a “Logoff” by the same user.
- Suspicious acts, such the deactivation of the antivirus followed by a program installation.
- Checking the privileges given to a process against the privileges of the user who started it and making sure the security policy is not violated.
A pattern $r$ is defined by the grammar:

$$
\begin{align*}
  r & ::= \\
  \epsilon & | \text{The empty sequence.} \\
  a.r & | \text{“a” followed by a pattern, “a” defined below.} \\
  a & ::= \\
  t & | \text{term of the term algebra with variables.} \\
  \lceil t \rceil & \text{term of the term algebra containing } t \text{ as a subterm.} \\
  x_r . r & | x_r \text{ represents any sequence of terms.}
\end{align*}
$$

- “$a$” represents single events in the log tree model
- “$a$” is either a term “$t$” of the algebra or a term containing “$t$” ($\lceil t \rceil$), it may contain variables.
- “$x_r$” represents a sequence of terms of zero or any finite length.
Examples of Patterns

The following are examples of patterns:

- \( \log x, \log y \), Logon\( (u_x, p_2, p_3, p_4, p_5, p_6) \), Logoff\( (u_x) \)

A sequence of events followed by a “Logon” of a user followed by another sequence then a “Logoff” by the same user.

We note here:

- We must distinguish between sequence variables \( (x_r, y_r, \ldots) \) and term variables \( (u_x, p_2, \ldots) \).
- We must distinguish between constants and variables and between sorts, \( p_2 \) to \( p_6 \) above are variables.
- If \( u_x \) is a variable then the pattern means a “Logon” by a user followed by a “Logoff” of the same user.
- If \( u_x \) is a constant then the pattern means a “Logon” by a specific user followed by a “Logoff” of the same user.
Examples of patterns (2)

- \( x_r. \lceil u_x \rceil . y_r. \text{Logoff}(u_x) \)
  Assume \( u_x \) is of sort user, then the pattern means:
  A sequence of events followed by any event involving the user \( u_x \) followed by another sequence then a “Logoff” by the same user \( u_x \).

- In the pattern above, \( x_r, y_r \) are sequence variables and \( u_x \) is a term variable.

Given a pattern like the above how do we match it to an actual sequence of the log tree?
⇒ Substituting sequence variables and term variables.
Examples of patterns (2)

- $x_r . \lfloor u_x \rfloor . y_r . \text{Logoff}(u_x)$
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Given a pattern like the above how do we match it to an actual sequence of the log tree?
⇒ Substituting sequence variables and term variables.
Searching for patterns

To look for pattern:
\[ x_r.Logon(u_x, \ldots).y_r.Logoff(u_x) \]

We have to find two substitutions:
1. for sequence variables \( x_r, y_r \) and
2. for term variables \( u_x \), such that:

Applying the substitutions to the pattern will result in a sequence in the tree.

In the example: \( u_x \mapsto Admin, x_r \mapsto \epsilon, \) and \( y_r \mapsto ProcessBegin(\ldots).ObjectOperation(\ldots).e_1.e_3 \) and so we can find one sequence that matches the pattern.
Searching for patterns

To look for pattern:
\[ x_r \cdot \text{Logon}(u_x, \ldots) \cdot y_r \cdot \text{Logoff}(u_x) \]

We have to find two substitutions:
(1) for sequence variables \( x_r, y_r \) and
(2) for term variables \( u_x \), such that:

Applying the substitutions to the pattern will result in a sequence in the tree.

In the example: \( u_x \mapsto \text{Admin}, \ x_r \mapsto \epsilon, \) and \( y_r \mapsto \text{ProcessBegin}(\ldots) \cdot \text{ObjectOperation}(\ldots) \cdot e_1 \cdot e_3 \) and so we can find one sequence that matches the pattern.
Need for Logic

- We need to be able to express more complicated properties of sequences, i.e., for every “Login” there is a “Logoff”, for this we use logic formulas.
- A formula is true for a certain model (log tree) $L$ if there are sequences “$s$” in $L$ that satisfy the property expressed by the formula.
- The semantics of a formula is taken to be the set of sequences of the log tree $L$ for which the formula is true.
Syntax of Logic

\[ \varphi ::= 
\begin{align*} 
Z & \mid \text{Formula variable.} \\
\neg \varphi & \mid \text{Negation.} \\
\varphi_1 \land \varphi_2 & \mid \text{Conjunction.} \\
[r_1 \leftrightarrow r_2]\varphi & \mid \text{All sequences in the log tree that match the pattern } r_1 \text{ and when modified to match } r_2 \text{ will satisfy } \varphi. \\
\llangle L \rrangle \varphi & \mid \text{Limits the search to events whose log source } l \in L \\
\nu Z.\varphi & \mid \text{The largest set of sequences that is a fixpoint of a semantic function mapping } Z \text{ to a set of sequences.} 
\end{align*} \]
We define the following:

\[ \neg (\neg \varphi_1 \land \neg \varphi_2) \equiv \varphi_1 \lor \varphi_2 \]

\[ \neg \varphi_1 \lor \varphi_2 \equiv \varphi_1 \Rightarrow \varphi_2 \]

\[ \neg [r_1 \Rightarrow r_2] \neg \varphi \equiv \langle r_1 \Rightarrow r_2 \rangle \varphi \]

\[ \neg \nu Z. \neg \varphi[\neg Z/Z] \equiv \mu Z. \varphi \]

Disjunction.

Implication.

There exists sequences in the log tree that match the pattern \( r_1 \) and when modified to match \( r_2 \) will satisfy \( \varphi \).

Least fix point, i.e., the largest set of sequences that is a fixpoint of a semantic function mapping \( Z \) to a set of sequences.

\[ \nu Z. Z \equiv \text{tt} \quad \text{True.} \]

\[ \mu Z. Z \equiv \text{ff} \quad \text{False.} \]
Examples of Formulas

Events

<table>
<thead>
<tr>
<th>Event</th>
<th>Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>Logon(Admin,...)</td>
<td>( t_0 )</td>
</tr>
<tr>
<td>ProcessBegin(...)</td>
<td>( t_1 )</td>
</tr>
<tr>
<td>ObjectOperation(...)</td>
<td>( t_2 )</td>
</tr>
<tr>
<td>e_0</td>
<td>( t_3 )</td>
</tr>
<tr>
<td>e_1</td>
<td>( t_4 )</td>
</tr>
<tr>
<td>e_2</td>
<td>( t_5 )</td>
</tr>
<tr>
<td>LogOff(Admin)</td>
<td>( t_6 )</td>
</tr>
</tbody>
</table>

Time

Formulas satisfied by the tree:

\[- \nu Z. [x_r.Logon().y_r.Logoff().z_r \Downarrow x_r.y_r.z_r] \rangle Z\]

\[- \langle x_r.e_1.y_r \Downarrow \epsilon \rangle tt\]

\[- \langle x_r.e_3.y_r \Downarrow x_r \rangle \langle x_r.e_3.y_r \Downarrow \epsilon \rangle tt\]
A tableau is a proof tree whose root is the formula to be proved.

Rules of the tableau indicate how the tree grows downward.

At some point we reach leaves of the tree.

Rules indicate when a leaf is considered successful.

A formula is proved if it has a successful tableau, i.e., all the leaves are successful.
Conclusion

- Model checking is proposed for log analysis.
- Logs are modeled as trees whose edges are algebraic terms.
- Properties of logs are expressed in a logic that deals with sequences of terms.
- A proof system is given to prove properties.